

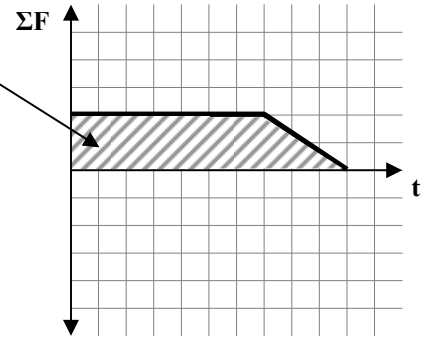
## Newton's Laws of Motion

- 1.) *An object in motion stays in motion, an object at rest stays at rest; inertia*
- 2.)  $\Sigma F = m \cdot a$
- 3.) *For every force, there is an equal and opposite force; forces always occur in equal and opposite pairs.*

## Impulse-Momentum

Sample Problem 1: Based upon the graph at right, if an object starts from rest and has a mass of 5 kg, what will be its final velocity?

Impulse (I) = area on  $\Sigma F$  vs. t graph  
 $I = 2\text{ N} \cdot 7\text{ s} + \frac{1}{2} \cdot 2\text{ N} \cdot 3\text{ s}$   
 $I = 14\text{ N}\cdot\text{s} + 3\text{ N}\cdot\text{s} = 17\text{ N}\cdot\text{s}$   
 Since I causes  $\Delta p$ ,  $I = m \cdot \Delta v$   
 $17\text{ N}\cdot\text{s} = (5\text{ kg}) \cdot \Delta v \rightarrow \Delta v = 3.4\text{ m/s}$   
 Since  $v_i = 0$ ,  $v_f = 3.4\text{ m/s}$



Sample Problem 2: If you (65 kg) jump at -2 m/s off a raft (120 kg) that is flowing at +1 m/s, what will be the raft's final velocity?

Mass and velocity info provided, no info about force or time  $\rightarrow$  use Conserv. of Mom.

$$p_{i\text{-system}} = p_{f\text{-system}}$$

$$p_{i\text{-you}} + p_{i\text{-raft}} = p_{f\text{-you}} + p_{f\text{-raft}}$$

$$m_y \cdot v_{i\text{-you}} + m_r \cdot v_{i\text{-raft}} = m_y \cdot v_{f\text{-you}} + m_r \cdot v_{f\text{-raft}}$$

$$(65\text{ kg}) \cdot (-2\text{ m/s}) + (120\text{ kg}) \cdot (1\text{ m/s}) = (65\text{ kg}) \cdot (-2\text{ m/s}) + (120\text{ kg}) \cdot (v_{f\text{-raft}})$$

$$185\text{ kg}\cdot\text{m/s} = -130\text{ kg}\cdot\text{m/s} + (120\text{ kg}) \cdot (v_{f\text{-raft}}) \rightarrow v_{f\text{-raft}} = +2.625\text{ m/s}$$

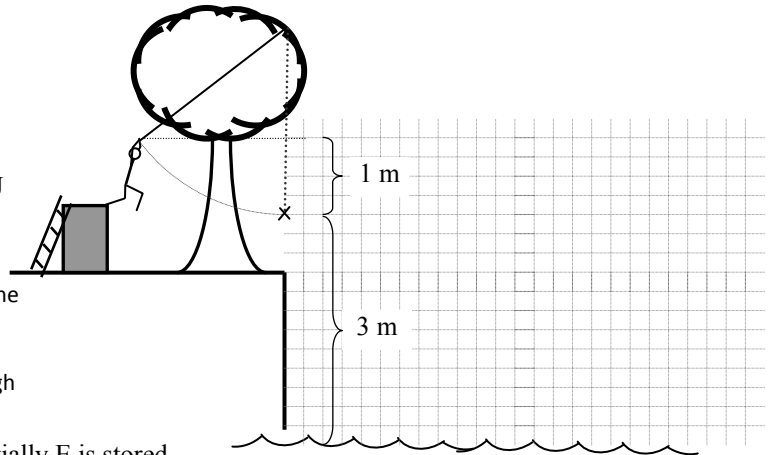
## Energy

Sample Problem 1: If you (65 kg) swing from the rope from rest, what will be your velocity at the "x"?

$E_{i\text{-system}} = E_{f\text{-system}}$ ; at highest point of swing, E is stored entirely  $E_g$ , at bottom of swing E is stored entirely  $E_k$ .

$$E_g = m \cdot g \cdot \Delta y = (65\text{ kg}) \cdot (9.8\text{ N/kg}) \cdot (1\text{ m}) = 637\text{ N}\cdot\text{m} = 637\text{ J}$$

Since in *this situation*  $E_g = E_k$ ,  $E_k = 637\text{ J} = \frac{1}{2} \cdot m \cdot v^2$   
 $\rightarrow v = 4.427\text{ m/s}$

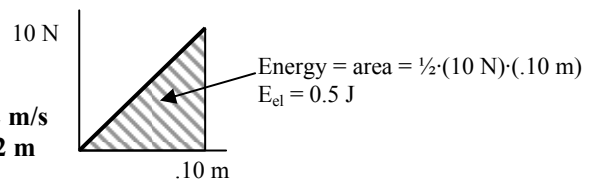


Sample Problem 2: A spring dart gun is loaded with a 50 g dart. The spring is compressed by 10 cm as the dart is loaded and this requires 10 N of force. How much energy is stored elastically? How fast will the dart be moving when it leaves the gun? How high will the dart go (if it's launched straight up)?

$E_{i\text{-system}} = E_{f\text{-system}}$ ; total E in system is constant value. Initially E is stored entirely  $E_{el}$ , when leaves gun all  $E_k$ , at highest point all  $E_g$ .

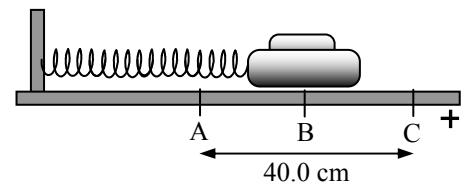
$$E_{el} = \text{area on } \Sigma F \text{ vs. } t \text{ graph} = 0.5\text{ J} \rightarrow E_{el} = 0.5\text{ J}$$

All this energy is then stored  $E_k$ , therefore  $E_k = \frac{1}{2} \cdot m \cdot v^2 = 0.5\text{ J} \rightarrow v = 4.472\text{ m/s}$   
 All this energy is then stored  $E_g$ , therefore  $E_g = m \cdot g \cdot \Delta y = 0.5\text{ J} \rightarrow \Delta y = 1.02\text{ m}$



## Oscillating Particle | Wave Fundamentals

Sample Problems: What is the hovercraft's amplitude of oscillation? If the period of oscillation is 1 second, and the spring constant is quadrupled, what will be the new period? ...what if the mass had been quadrupled?



$$A = 20\text{ cm} = 0.20\text{ m}$$

T depends on square root of the inverse of spring constant, so changing the spring constant by a factor of 4 will change the period by a factor of square root of  $\frac{1}{4}$ , which is  $\frac{1}{2}$ .

T depends on square root of mass, so changing the mass by a factor of 4 will change the period by a factor of square root 4, which is 2.

## Matter Waves

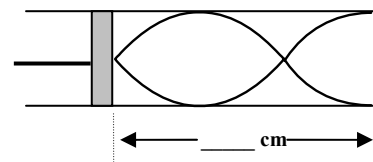
Sample Problems: How many nodes are in the standing wave pattern? How many antinodes? How much of a wave is present? If the end-to-end distance is 6 meters, then what is the wavelength? If the resonant frequency for this situation was doubled, what would be the new wavelength? If a standing wave pattern with a wavelength of 3 meters was produced by a resonant frequency of 4 Hz, what is the speed of the waves through the string?



4 nodes, 3 antinodes,  $3/2$  of a wave. In this situation,  $L = 3/2 \cdot \lambda \rightarrow \lambda = 2/3 \cdot L = 2/3 \cdot 6 \text{ m} \rightarrow \lambda = 4 \text{ m}$   
 Doubling frequency causes wavelength to be half, since they are inversely proportional.  
 Using the wave equation,  $v = f \lambda = (4 \text{ Hz}) \cdot (3 \text{ m}) \rightarrow v = 12 \text{ Hz} \cdot \text{m} \rightarrow v = 12 \text{ m/s}$

## Sound Waves

Sample Problem 1: What mode is represented in this tube? If the wavelength is 92.0 cm and the resonant frequency is 388 Hz, what is the speed of sound in this tube? What is the end-to-end length of the tube?

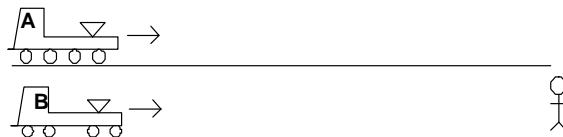


Mode 2.

Since  $v = f \lambda = (388 \text{ Hz}) \cdot (.920 \text{ m}) \rightarrow v = 356.96 \text{ m/s}$

Since this represents  $3/4$  of a wave,  $L = 3/4 \cdot \lambda = 3/4 \cdot (.92 \text{ m}) \rightarrow L = .69 \text{ m}$

Sample Problem 2: Two trains carry identical whistles that emit a sound with a frequency of 500 Hz when measured at rest. The trains approach an observer standing between two sets of tracks (see sketch) at velocities  $v_A = 40 \text{ m/s}$  and  $v_B = 20 \text{ m/s}$ . What are the frequencies that the observer will hear? What will be the beat frequency? Train A then passes the observer and is moving away while Train B is still approaching. What will be the beat frequency heard by the observer?



Doppler shift:  $f' = f \left[ \frac{v_{\text{waves}} + v_{\text{observer}}}{v_{\text{waves}} - v_{\text{source}}} \right]$

From Train A:  $f'_A = 500 \text{ Hz} \left[ \frac{(345 \text{ m/s} + 0)}{(345 \text{ m/s} - +40 \text{ m/s})} \right] = 565.57 \text{ Hz}$

From Train B:  $f'_B = 500 \text{ Hz} \left[ \frac{(345 \text{ m/s} + 0)}{(345 \text{ m/s} - +20 \text{ m/s})} \right] = 530.77 \text{ Hz}$

$f_{\text{beats}} = |f_1 - f_2| = |565.57 \text{ Hz} - 530.77 \text{ Hz}| \rightarrow f_{\text{beats}} = 34.8 \text{ Hz}$

Once Train A passes the observer, its frequency will be heard as  $500 \text{ Hz} \left[ \frac{(345 \text{ m/s} + 0)}{(345 \text{ m/s} - -40 \text{ m/s})} \right] = 448.05 \text{ Hz}$

$f_{\text{beats}} = |448.05 \text{ Hz} - 530.77 \text{ Hz}| = |-82.72 \text{ Hz}| \rightarrow f_{\text{beats}} = 82.72 \text{ Hz}$